



Forum on the Future of Interactive Multiobjective Optimization

Hybridizing Interactive Multiobjective Methods

Past Experiences and Future Trends

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Outline

- 1 Motivation
 - Interactive Techniques
 - How to choose an Interactive Method
- 2 Two Real Applications
 - Determination of Electricity Mix in Andalucía
 - Optimal Size of a Solar Thermal Plant
- 3 Conclusions and Future Trends

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It is a resolution method for Multiobjective problems, where the information exchange between the decision maker and the analyst is carried out in a continuous way during the resolution process. The method progressively incorporates the information given by the Decision Maker so as to lead him to his most preferred solution. Interactive techniques are specially suitable for favoring learning processes for both the decision maker and the analyst.

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Basic Scheme of Interactive Methods

Steps of an Interactive Method

- 1 Generate initial efficient solution(s)
- 2 Present the current solution(s) to the DM
- 3 Is the DM satisfied with some solution?
 - ✓ If "Yes", then end.
 - ✓ If "No", go to step 4
- 4 Ask the DM for preferential information
- 5 Generate new efficient solution(s)
- 6 Go to step 2

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What Type of Information may be Asked to the DM?

Types of Interactive Methods according to the information required

- Comparison Methods
 - ✓ Pair-wise comparisons
 - ✓ Several objective vectors
- Trade-off or local weights methods
 - ✓ The DM evaluates objective tradeoffs
 - ✓ The DM estimates subjective tradeoffs
- Level specification methods
 - ✓ Interactive Goal Programming methods
 - ✓ Reference Point based Methods
- Classification methods
- Non trading-off methods

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How do Interactive Methods Calculate New Solutions?

Types of Interactive Methods according to the optimization procedure

- Reduction of the feasible region
- Reduction of the weights space
- Feasible direction, line search
- Cutting planes (tradeoffs)
- Lagrange multipliers (constraint problems)
- Achievement scalarizing functions
- Steps towards the efficient frontier

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Desirable Properties (Afsar et al., 2021)

Topics

- **Easiness** to use.
- Cognitive burden.
- Sense of **being in control**.
- Ability to **capture preferences**.
- **Learning** about trade-offs.
- **Satisfaction and confidence** in the final solution.

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A single method may not have all these properties

- Importance of **assessing methods**.
- Different methods may **perform better at different stages**.
- Choosing an interactive method **is not trivial**.

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Our Conclusion as Analysts

What do WE have to do?

- We have to **choose a method**:
 - ✓ For each **problem**
 - ✓ For each **Decision Maker**
- We need to offer a **flexible framework**:
- We will probably need to **combine interaction styles**.
 - ✓ Hybridize different interactive methods.
 - ✓ Application 1.
- We will probably need to **combine solving techniques**.
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Main Features of the Study

Purpose

- Determine the **most preferred electrical mix** to cover the demand of Andalucía, taking into account economic, environmental and vulnerability criteria.
- **Evaluate the cost** of moving towards a more sustainable mix.
- DM: **Regional Ministry of Environment** of Andalucía.



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Elements of the Model

Variables

- 8 electricity generation systems: Lignite, Carbon, Oil, Natural Gas, Nuclear, Photovoltaic, Eolic, Hydraulic.

Y_j : Installed capacity (GW) for system j

- Demand: 108 time periods (t_k , hours), with a given hourly demand (d_k , GW).

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Elements of the Model (Cont.)

Constraints

- **Diversification & security.**
- Satisfaction of the demand.
- Electricity permanent availability.
- Technical constraints.

Objectives

- Cost
 - Fuel (Imported Fuel)
 - Variable O&M
 - Fixed O&M
 - Investment Costs
- Vulnerability (Percentage of Imported Fuel).
- Environmental Objectives.
 - CO₂ emissions
 - Air Quality

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 - ✓ Fixed annualized costs.
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 - ✓ 12 Impact Categories.
 - ✓ Life Cycle Analysis.

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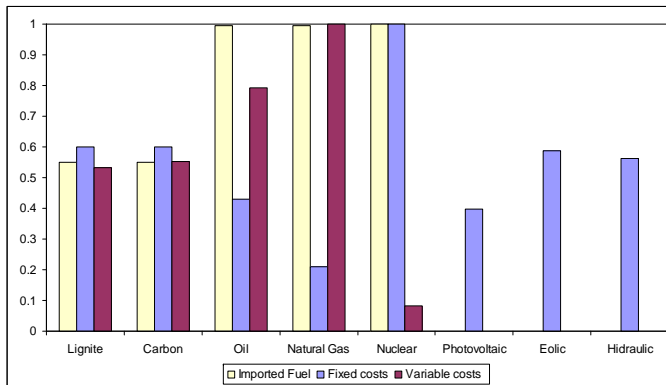
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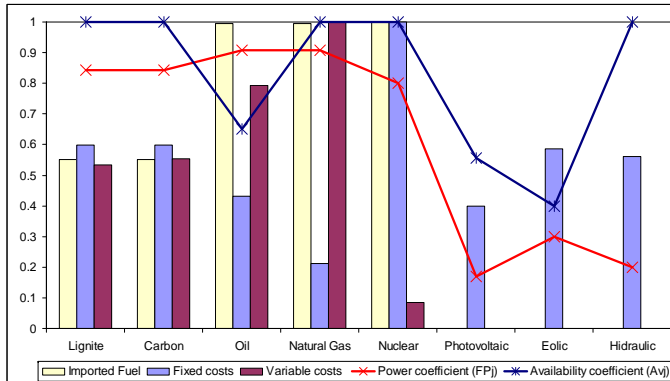
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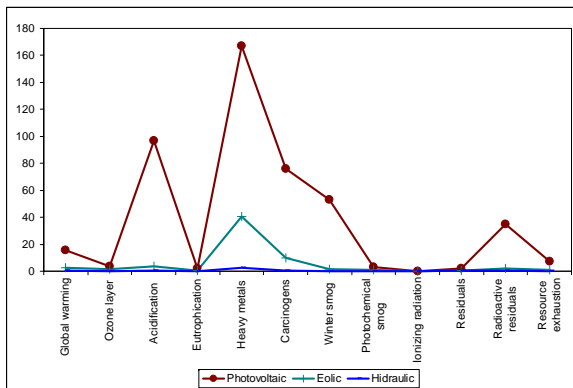
Cost and Vulnerability: Comparison of Alternatives



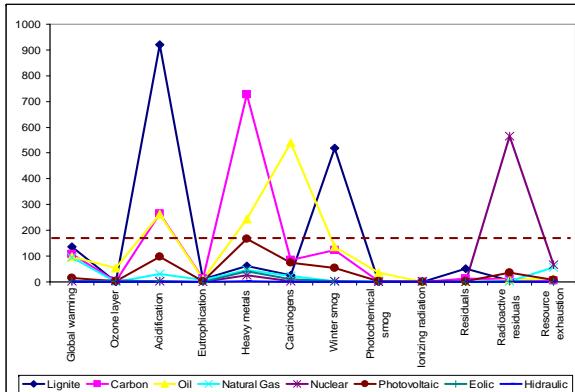
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Impact Categories: Comparison of Alternatives



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Model and Iterations

Features of the Linear Model

- 116 Variables.
- 1098 Constraints.
- 14 Objective Functions.

PROMOIN (Caballero, Luque, Molina, Ruiz, 2002). Iterations

- Initial Solution: minimum cost.
- Weighting of Objectives.
 - Cost & Value of the α Basis variable
- Reference Points and Classification.
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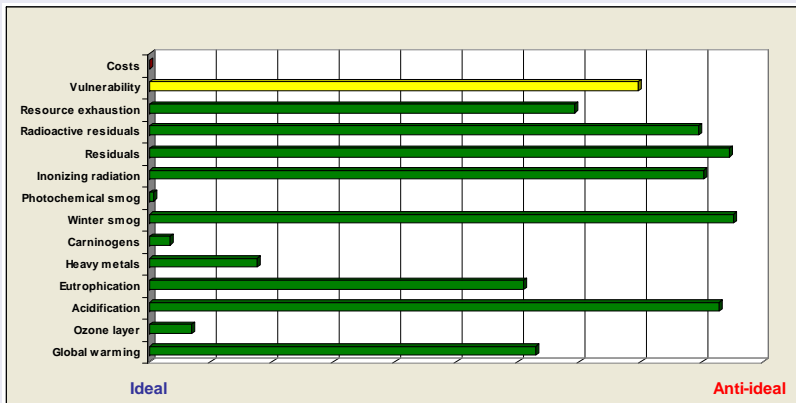
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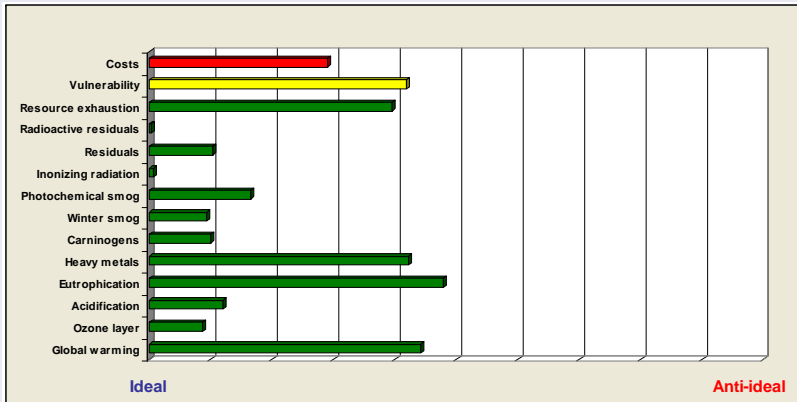
Results-Objectives

Minimum Cost



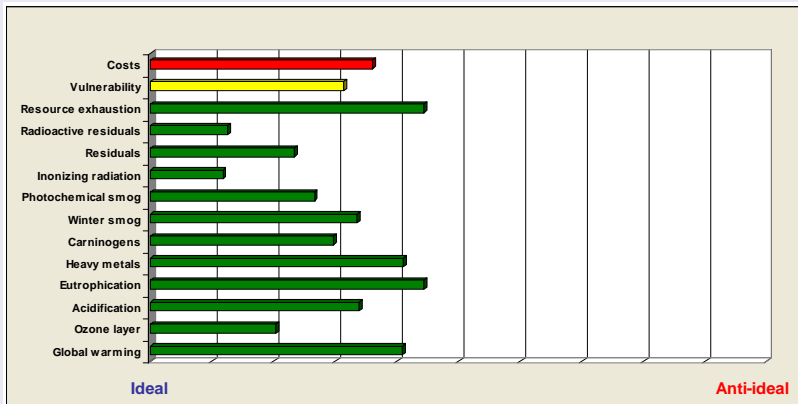
Results-Objectives

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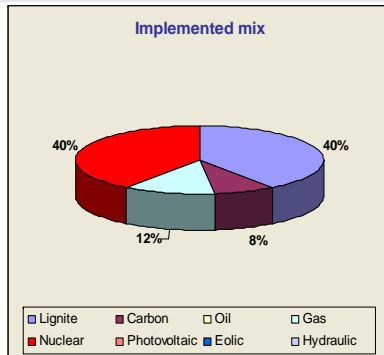
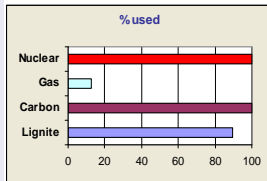
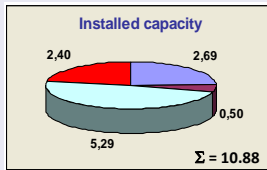
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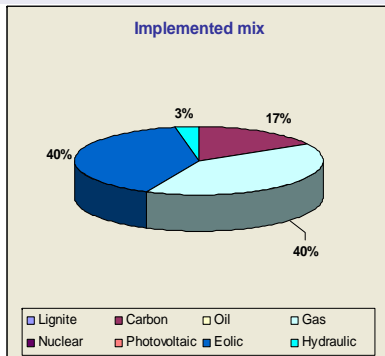
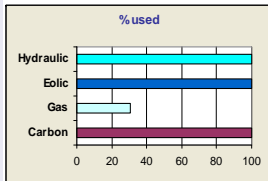
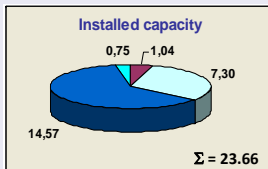
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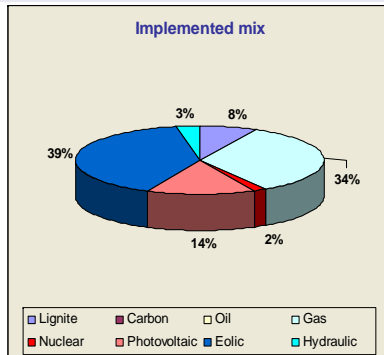
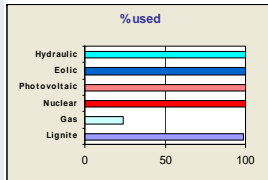
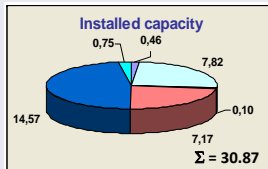
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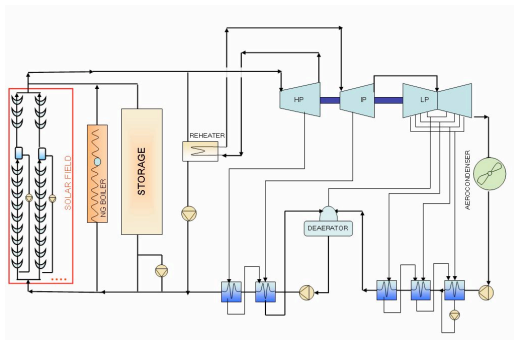


Purpose of the Study

Optimal Dimensions

- Solar Field
- Storage Tanks
- Auxiliary Boiler

Endesa Generación
S.L.

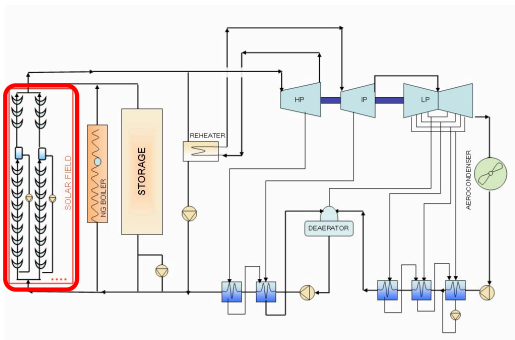


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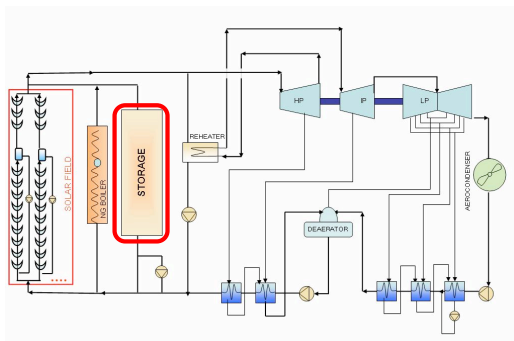


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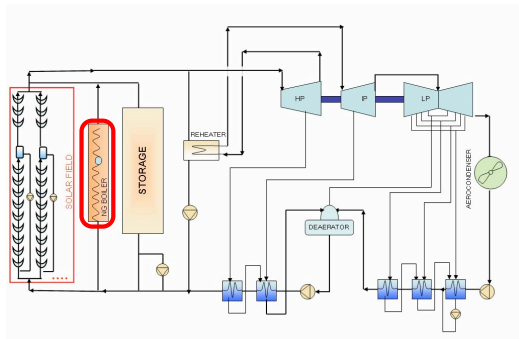


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Endesa Generación
S.L.



Elements of the Model

Variables

- A_C (m^2) Dimension of the Solar Field
 - ✓ File with **expected direct solar radiation** and temperature per hour (8760 hours) available. We determine the **steam mass from the solar field** at each hour.
 - ✓ $A_C \leq 750,000m^2$
- E (KJ) Capacity of Storage Tanks
 - ✓ One tank **maximum capacity**: 8 hours.
 - ✓ One tank **fixed cost**: 15 million €.
- P_{AUX} (KW) Power of the Auxiliary Boiler
 - ✓ **Legal limit**: 15% hybridization.
- L (%) Load Fraction Limit
 - ✓ $L \leq 75\%$.

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Why is the Problem so Complex?

Operation Strategy

Every hour, the following decisions are made:

- 1 If **steam mass** from the solar field is **enough to work at L** or more, work only with solar field.
 - ✓ If steam mass produces more than $L = 100\%$, store remaining steam.
- 2 If steam mass is not enough for L , and there is **enough energy stored**, complement to work at L .
 - ✓ Ambient losses in the tanks are taken into account.
- 3 If steam mass and storage are not enough for L , test **hybridization** condition.
 - ✓ If it is possible to hybridize with the auxiliary boiler, work at L .
 - ✓ If not, store steam mass from the solar field and stop plant.
 - ✓ After a 8 or more hours stop, the electricity produced is devoted to re-starting the system.

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Why is the Problem so Complex? (Cont.)

Black Box

- **Operation strategy is simulated** in a black box.
- We keep track of auxiliary variables.
 - ✓ E_i Energy stored after hour i .
 - ✓ $FUNC_i$ Load fraction of hour i .
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- **Hybridize with meta-heuristic techniques.**

Yearly Profit

- **Incomes.**
 - ✓ REV_i Revenue of hour i .
 - ✓ REV_{fix} Fixed selling price.
 - ✓ REV_{var} Variable selling price.
- **Fixed costs.**
 - ✓ FC_{fix} Fixed investment costs.
 - ✓ FC_{var} Variable investment costs.
 - ✓ FC_{oper} Operational costs.
- **Variable costs.**

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Yearly Profit

- Incomes.
 - Revenue
 - Fuel
 - Electricity
 - Heat
 - Biomass
 - Wind
 - Solar
- Fixed costs.
 - Investment
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 - Maintenance
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 - Other
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- Incomes.
 - ✓ 8760 hourly incomes.
 - ✓ Based on $FUNC_i$.
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 - ✓ Annualized installation costs.
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Optimizing Yearly Profit

(Deb, Tewari, <http://www.iitk.ac.in/kangal/soft.htm>)

GA Solution

● Variables.

- ✓ $A_C = 750,000$
- ✓ $E = 15.68$ hours (2 tanks)
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● Profit 29,201,020 €

● Other Features

- ✓ Investment: 406,769,471 €
- ✓ Internal rate of return: 13.32%
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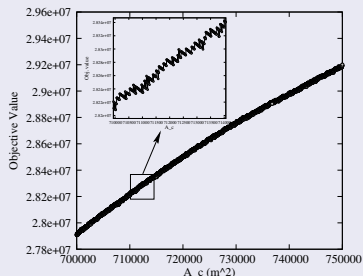
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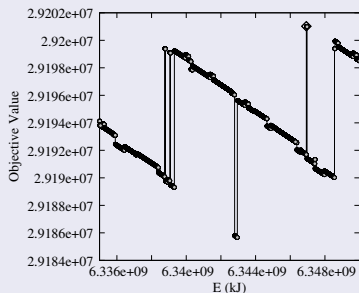
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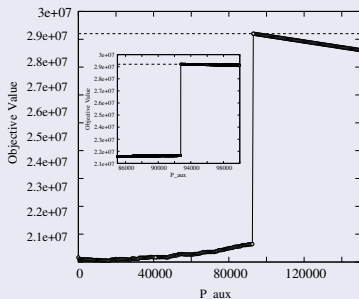
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The Multiobjective Model

Objectives

- Maximize Profit.
- Minimize Investment.
- Maximize IRR.
- Minimize Pollution.

Resolution Process

- Individual optima (GA).
- Efficient Front: NSGA-II (Deb et al, 2002).
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Individual Optima

What we learnt

- Optimal investment cost.
 - ✓ No activity.
 - ✓ The cost of the tanks is the highest component.
 - ✓ Lower values of L are better.
- Optimal IRR.
 - ✓ Maximum of 16.16%, with $E = 0$ and $L = 25$.
 - ✓ For non-zero values of E , maximum IRR is around 14.84%.
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 - ✓ Small A_G and small L .
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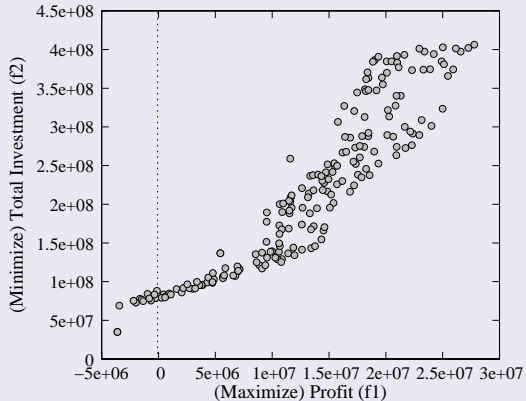
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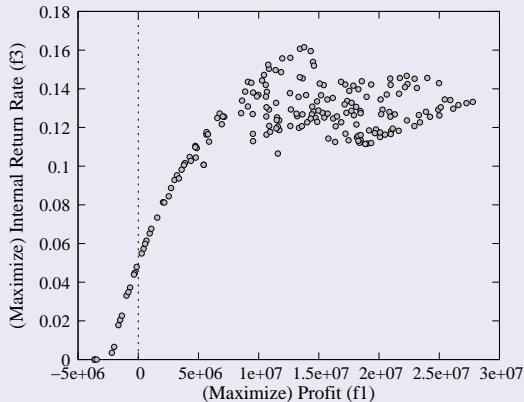
Efficient frontier - What we learnt

Profit vs. Investment Cost



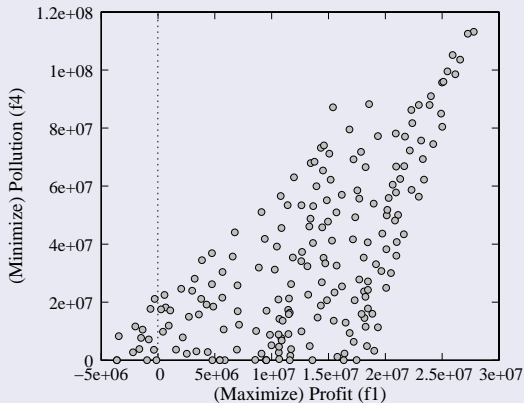
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Profit vs. IRR



Efficient frontier - What we learnt

Profit vs. Pollution



Final Approach: Reference Point Based NSGA-II + GA

Initial Variables

- $A_C = 750,000$
- $E = 15.68$ hours (2 tanks)
- $P_{AUX} = 92,768$
- $L = 75.00$

Final Variables

- $A_C = 490,312$
- $E = 6,39$ hours (1 tank)
- $P_{AUX} = 90,261$
- $L = 63,52$

Decision Variables



Final Approach: Reference Point Based NSGA-II + GA

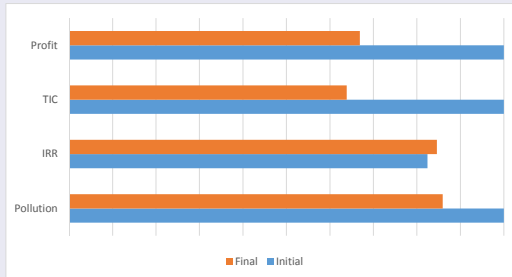
Initial Objectives

- Profit 29,201,020.
- TIC: 406,769,471.
- IRR: 13.32%.
- Pollution: 58,125,795.

Final Objectives

- Profit 18,596,015.
- TIC: 259,779,783.
- IRR: 13.67%.
- Pollution: 49,956,127.

Objective Functions



What is Needed in Real Applications?

3 Lessons Learned

- There is no such thing as “the best interactive method”
- **Flexibility** is extremely important
 - ✓ Importance of intuition.
 - ✓ Pay attention to “primary” responses or reactions of the DM.
 - ✓ Possibility to combine different methods.
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Interactive MOP as a Learning Process

We all Learn

- The **modelling** process itself **is a rich learning phase** for both the analyst and the DM.
- During the **interactive learning phase**, we learn:
 - ✓ About the **structure of the feasible set**.
 - ✓ About the **tradeoffs among the objectives**.
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- It is **only this learning process** what makes the analyst and DM **confident** about the final solution obtained.

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Hybridizing different interactive methods

- Use the **most appropriate type of interaction** for each problem, DM, and phase.
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And more future trends

...See the panel discussion tomorrow!

Thank you!

**Thank you very much
for your kind attention**